

# CENTRE COURT APARTMENTS STATE COLLEGE, PA

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## **Executive Summary**

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This report was conducted with the intent of comparing the current as build structural system of the Centre Court Apartments to four other structural systems applied to the same building. Following design of the system they will be compared and contrasted for their varying qualities of weight, constructability, thickness of system, MEP compatibility, fireproofing, and vibration effects. The original system was made of 8" Precast Hollow Core Plates topped with a 3"-5.5" layer of concrete bearing mostly on CMU's. The four structures this was compared against were:

1. Two Way Post Tension Slab
2. Composite Lightweight Concrete Slab on Steel Frame
3. Two Way Flat Slab
4. Waffle Slab

Each structure had many benefits such as the ease of construction of the hollow core planks and the waffle slabs, or the thinnest slab offered by the post tension system. Although, following the technical evaluation of all the structures against the criteria listed about it was found that the two systems worth exploring further in detail were the composite lightweight concrete slab on steel frame and the two-way flat slab. Both systems are very familiar in the industry and also lend themselves well to the short spanning varying geometry of the spans in the Centre Court Apartments.

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## Existing Structural System

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Listed below are the prominent structural elements contained in Centre Court Apartments:

- 8" CMU exterior above grade and 10" CMU exterior below grade
  - Load bearing units conforming to ASTM C90
  - Net Compressive Stress = 3000 PSI
  - Above grade CMU's contain Dur-O-Wall every other course
  - Block cells with bars are grouted a minimum 2 courses below plank bearing
  
- 8" pre-cast hollow core planks
  - Conform to latest edition of ACI 318
  - Steel bearing will contain weld plates spaced 4' O.C. max.
  - $F'_c=5000$  PSI
  
- Steel beams and columns
  - Typical beam sizes: 12 X 26 and 14 X 43
  - Grade 50 or ASTM A992
  - Fabricated and erected in accordance to the latest edition of AISC specifications.
  
- Concrete columns, footings, and slabs
  - Mixed and placed in accordance with ACI 318 "Building Code Requirements for Concrete"
  - Footings and slabs  $f'_c = 3000$
  - Columns  $f'_c = 4000$

The load-bearing CMU exterior walls dominate the structural design. This system also crosses north to south at particular portions of the interior building in order to be the primary lateral force resisting system. This structure has a number of benefits in the Centre Court Apartments. The added convenience of bearing the pre-cast hollow core slabs. Pre-cast hollow core concrete slabs make up at least 90% of all floor slabs in the building and the concrete to concrete block connection cuts down on the number of bearing plates that would be needed if the number of slab to steel connections were increased.

Another benefit of this system is the simplification of the beam to column connections throughout the building. Since no moment frames are required, all moment connections have been completely elevated from the building. There

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are also two non-structural benefits to the CMU design: the fire rating requirements for apartment buildings and the way it compliments the application of the aesthetic stucco applied to the exterior of the building.

The remaining interior loads are carried by a series of wide flange beams, which distribute that load to steel columns in the top five floors. The bottom two levels of parking deck then convert to concrete columns, which at the end drop the load onto the 6' X 8' spread footings.

**Advantages and disadvantages to this system:**

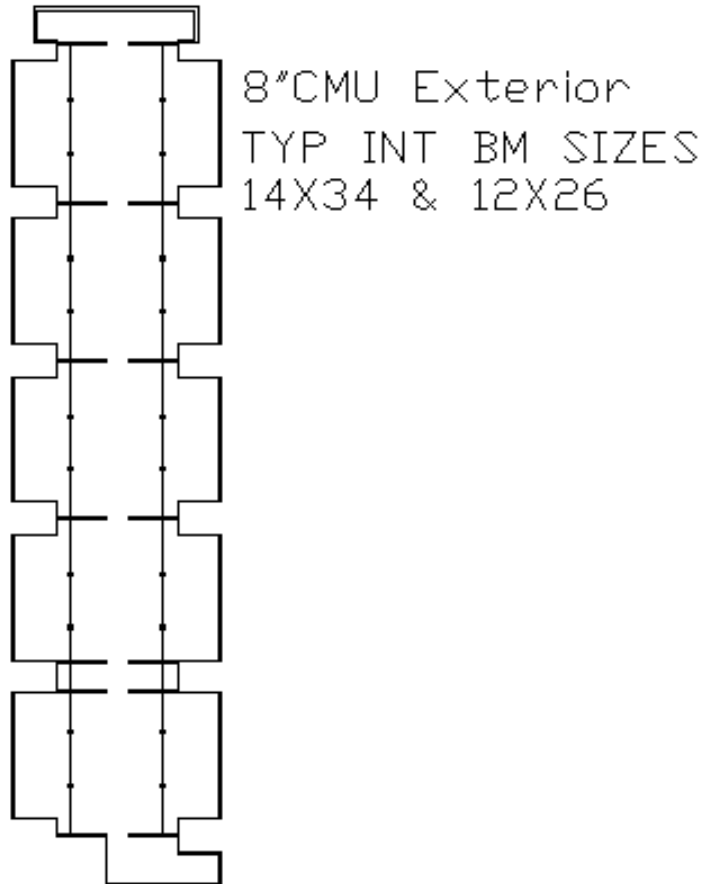
Being that the structure is an apartment complex architectural freedom is very important. With the precast hollow core slab design that bears a great deal on the exterior walls the intrusion of columns is decreased greatly. The Hollow core slabs also decrease on site construction time by a great deal, although a longer lead-time is often a direct cost of this trait. Including the 3-5.5" concrete topping the floor structural system can be 13.5" thick at points, which is a moderately thick floor structure for this building.



The Hollow core slabs in conjunction with the CMU wall offer excellent fire protection benefits. This combination also aids well to noise dampening which are both strong benefits to an apartment complex. Studies also show that insurance rates for buildings incorporating either of these technologies tend to be less than other structural options.

## Existing Structural Plan

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## Codes and References

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- The International Building Code 2003
- The American Concrete Institute
  - Section 530.1: Masonry
- The American Institute of Steel Construction
- CRSI 2002: Concrete Reinforcing Steel Institute
- United Steel Deck Design Manual 2002

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## Loads

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Gravity Loads have been calculated in accordance with ASCE 7-05 with the Live Loads interpreted from section four. Assumptions were made for proper distribution of Gravity Loads.

### Dead Load

Hollow Core Planks	60	psf
Concrete	150	pcf
Partitions	15	psf
MEP	10	psf
Misc.	5	psf
Brick	38	psf
8' CMU	60	psf
Windows	8	psf

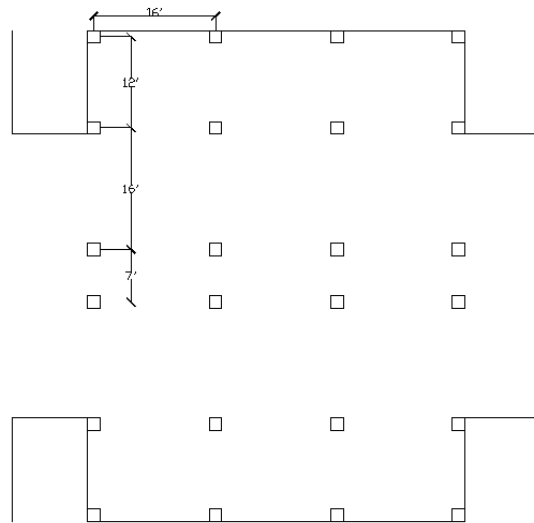
### Live Loads

Corridors	100	psf
Garages	40	psf
Private Rooms	40	psf
Public Rooms	100	psf
Roof	20	psf
Snow	21	psf

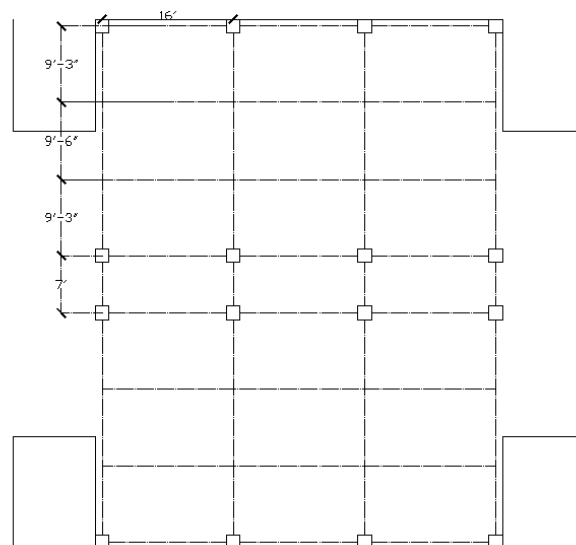
## Alternative Designs

There were four alternative design methods tested for this technical assignment, post tensioned two way flat plate, composite light weight concrete slab on steel frame, two way flat slab, and a waffle slab design. The strict architectural layout minimizes the diversity of column arrangement strategies. The plans below show the most functional column layout applicable to a redesign of the system. All Concrete columns in the below plans are taken as 20"X 20" to keep uniformity with the parking deck below.

### Concrete Design:



### Steel Design:





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## Post Tensioned 2 Way Flat Plate

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Post Tension concrete is traditionally used to span long distances with minimal thickness increases and also to minimize visual cracking in such spans. Although, due to the architectural layout of the Centre Court Apartments discussed above this system was tested over moderately sized spans with an attempt to see if the decreases in thickness would be worth the costs of this system even with the shorter span lengths.

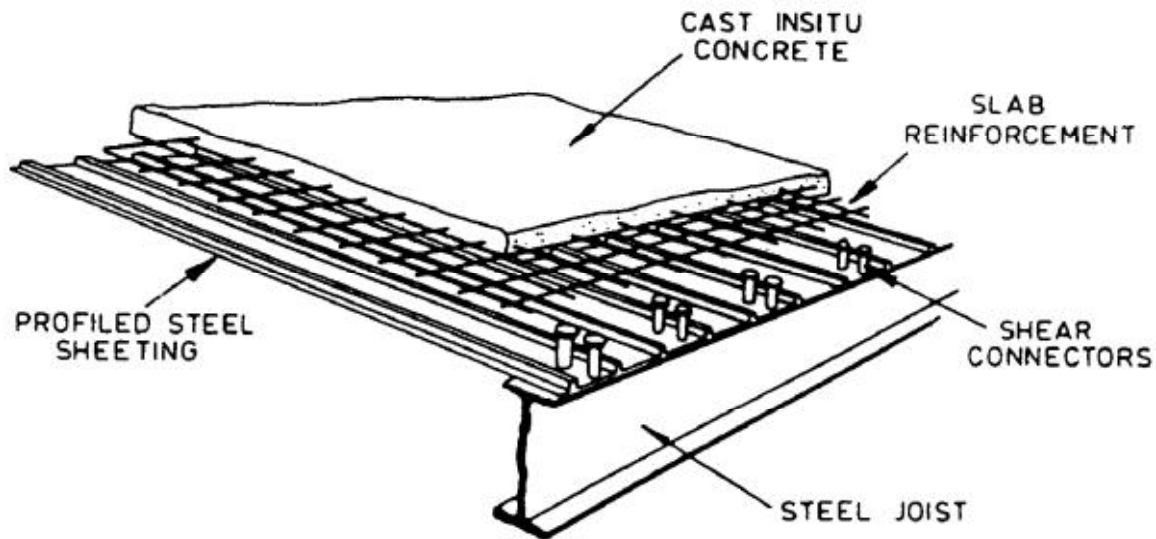


### **Advantages and Disadvantages to this system.**

The slab analysis resulted in a 5 in slab. This is severely less than the current system although due to this extreme decrease in depth the punching shear surrounding the columns requires extra shear reinforcement which will certainly counteract some of the savings due to decreased amount of concrete. From a construction standpoint not all contractors work well and are comfortable with post tension slabs. If not installed correctly the extreme force applied to this system shortly after construction can result in very dangerous situations. Although as long as an expedited crew is obtained it should be a very viable solution.

## Composite Light Weight Concrete Slab on Steel Frame

The composite lightweight slab on steel frame system is a standard system in the industry. The system can adapt to all kinds of floor framing layouts with ease, which obviously benefits the Centre Court Apartments architectural plan. This system was analyzed with an attempt to use the moderately thin slab it affords in conjunction with lightweight concrete to not only minimize floor to floor height but more importantly the dead load of the building as a whole.



### Advantages and disadvantages to this system:

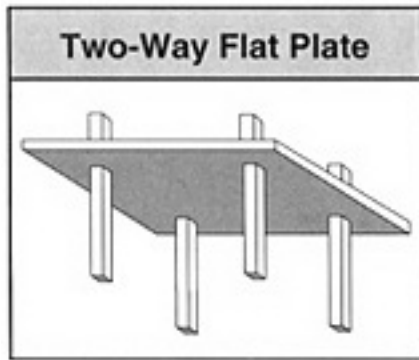
Many contractors work well with the slab on steel frame system because it is very commonplace in the industry. The slab depth came out to be 5.25" being only .25" thicker than the post tension design. This along with the 115pcf lightweight concrete does a lot in decreasing the load of the slab bearing on the structure. Vibration can be a concern with the steel system and should be given optimal attention due to its high level of impotence in an apartment complex such as this and additional fireproofing with certainly be needed to cover the steel. Those disadvantages aside the concrete slab on steel frame appears to be a viable alternative.

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## 2 Way Flat Plate Slab

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The two way flat plate design is most likely the most convenient and feasible for the short span lengths of the Centre Court Apartments. The design hopes to only increase the slab thickness slightly from the post tension design and steel deck slab design while taking advantage of the short spans by alleviating the need for drop panels or additional shear reinforcement. The Equivalent frame method was used in analyzing the system and although the slab could have shortened its thickness in the interior spans, the change was not that drastic and the design was kept constant for ease of construction.



### Advantages and disadvantages of this system:

Although assembly and disassembly of formwork for a job of this size can be very timely and costly to a contractor and owner will once again rarely find a contractor who's team doesn't have the ability or is not familiar with this system. No additional fireproofing is needed and the vibration effects are also much better than that of the slab on steel decking system. The 6.5" depth is by no means in a situation to cause building height issues and because the punching shear design does not require drop panels the MEP system can scale along the system with ease.

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## Waffle Flat Slab

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Waffle slab systems are often incorporated because although they often add a lot of thickness compared to their alternatives they, more times than not will decrease the weight of the structure dramatically. The system is also most applicable over large spans, which, as discussed above, is definitely not the case with the Centre Court Apartments. The system was selected through design tables out of the Concrete Reinforcing Steel Institute Design Guide of 2002. The slabs have 19" x 19" voids with 5" ribs at 24" O.C.. The rib depth also came out to be 8" with a slab depth of 3".



### **Advantages and disadvantages to this system:**

Waffle slabs have very similar characteristics to the existing structure of hollow core floor planks in the area of construction and lead-time. That being, simpler and faster construction methods as compared to other systems although a longer setting-on-site time due to the nature of the product. Waffle slabs often compliments MEP systems well and the vibration effects that are mitigated by such an assembly are very good as well. On the other hand waffle slab construction is not typically designed for a building whose bays are constantly alternating in size. I designed the slab for the maximum span although when all is said and done, if preferred, many sizes and shapes of waffle slabs could technically be incorporated in this design. At least to alternative sizes would be practical from a construction standpoint. I also found that the weight saved by the system was not significant enough to justify the increase in thickness.

## Comparison

	<b>Hollow Core  Planks</b>	<b>Comp. Slab on Steel Deck</b>	<b>2 Way Flat Plate</b>	<b>Post T.</b>	<b>Waffle Slab</b>
<b>Weight</b>	96 psf	62 psf	81 psf	62.5 psf	95.7 psf
<b>Thickness</b>	13.5 "	5.25 "	6.5 "	5 "	11 "
<b>Vibration</b>	no	yes	no	no	no
<b>Additional Fire Proofing</b>	no	yes	no	no	no
<b>Const. Difficulties</b>	no	no	no	yes	ye
<b>Lead Time</b>	yes	a little	no	no	yes
<b>Amount of Form Work Acceptable Alternative</b>	none	good amount	a lot	a lot	none
		yes	yes	no	no

## Conclusion

Following analysis of the 5 methods, four alternatives and one existing I found that each of them have many individual advantages but also drawbacks as compared to the other methods. The thinnest slab was obtained with Post tension, although the savings in the end were not that significant compared to the other methods and the technical experience needed on such a project most likely is not necessary for this building with its smaller spans. The Waffle slab did not end up saving weight in the long run and as well as the existing structure its thickness and lead time were not completely justified in the end. The ease of construction and adaptability to the span geometry of the slab on steel decking gave positive results and is worth continuing research on in the future. Although the final conclusion stands with the two way flat plate slab. This system is relatively thin, light, easy to construct, and won't be terribly expensive. It can take economic benefit from the varying slab size changes and at this point will be the top selection for further review.

## **Appendix**

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**Post Tension Two Way Flat Plate**  
**Composite Lightweight Concrete Slab on Steel Frame**  
**Two Way Flat Plate**  
**Waffle Slab**

POST TENSIONED 2 WAY FLAT PLATE

20 x 20 COL'S  
 $f'_c = 3,000 \text{ PSI}$   
 $f_y = 60 \text{ KSI}$   
 $f_{pu} = 270 \text{ KSI}$  1/2" DIAMETER TENDONS  
 $A_t = 0.53 \text{ in}^2$

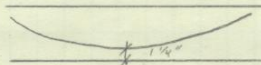
16' MAX SPAN

SPAN/DEPTH RATIO = 45

$$\frac{16 (12'')}{45} = 4.26 \Rightarrow \text{TRY } 5'' \text{ SLAB}$$

$$d = 5 - .75 = 4.25$$

1/4" #



1" CLR AT TOP & BOTTOM FOR 2 HR FIRE RATING

$$a = 5 - 2(1.25) = 2.50''$$

LOADS  
 DL: SLAB -  $5 \left(\frac{1}{4}\right) 150 = 187.5 \text{ PSF}$   
 MEP 10 PSF  
 PARTITIONS 15 PSF  
 MISC 5 PSF  
92.5 PSF

LL: 40 PSF

BANDED TENDONS IN THE EAST-WEST DIR.  
 UNIFORM TENDONS IN THE NORTH-SOUTH

$$W_{PRE} = 0.9(62.5) = 56.25 \text{ PSF}$$

$$W_{NET} = 132.5 - 56.25 = 76.25 \text{ PSF}$$

$$M_{PRE} = \frac{56.25 (16')^2}{8} = 1800 \text{ ft-k}$$

$$F = \frac{M_{PRE}}{a} = \frac{1800 (12)}{2.5} = 8.46 \text{ K}$$

$$F/A = \frac{8.46 (1000)}{60} = 141 \text{ PSI}$$

$$A = 5'' (12'' \text{ STRIP}) = 60 \text{ IN}^2$$

BUNDLES AT STRIP IN E-W DIRECTION

$$M_o = \frac{(0.07625)(16')^2}{8} = 2.4 \text{ ft-k}$$

$$M^- = .65(2.4) = 1.56 \text{ ft-k}$$

$$M^+ = .35(2.4) = 0.84 \text{ ft-k}$$

2

AVG STRESSES

$$S = 2(5^2) = 50 \text{ IN}^3$$

STRESS LIMITS

SPAN ENDS:  $f_c = 6\sqrt{f_c} = 328.63$   
 MID SPANS:  $f_c = 3\sqrt{f_c} = 124.3$   
 $f_c = 0.45 f_c = 1350$

$$S = \frac{F}{k} = \frac{M_D}{S}$$

$$M_u^-: \quad f = -141 \text{ PSI} \pm \frac{1.56(12)(1000)}{50} = \begin{matrix} 233.4 < 328.63 \\ -515.4 < 1350 \end{matrix} \checkmark$$

$$M_u^+: \quad f = -141 \text{ PSI} \pm \frac{0.84(12)(1000)}{50} = \begin{matrix} 60 < 124 \\ -342.6 < 1350 \end{matrix} \checkmark$$

BUNDLES @ STRIPS IN E-W

$$F = 8.46 \text{ KIP} (16) = 135.36$$

$$N_T = \frac{135.36}{(270)(0.153)} = 3.28 \Rightarrow \text{USE 4 TENDONS EACH WAY}$$

NORMAL REINFORCEMENT DESIGN

D L SLAB  $0.1(62.5) = 6.25 \text{ PSF}$   
 MOB, PART, MISC  $= 30 \text{ PSF}$   
36.25 PSF

LL = 40 PSF

$$W_u = 1.2(36.25) + 1.6(40) = 107.5$$

$$M_D = \frac{W_u l^2}{8} = \frac{107.5(16')(16 - \frac{30}{12})^2}{8} = 44.17 \text{ IN}$$

$$M_u^- = .65(44.17) = 28.7 \text{ IN}$$

$$M_u^+ = .35(44.17) = 15.5 \text{ IN}$$

$$CS M_u^- = .75(28.7) = 21.53$$

$$MS M_u^- = .25(28.7) = 7.18$$

$$CS M_u^+ = .63(15.5) = 9.77$$

$$MS M_u^+ = .37(15.5) = 5.74$$



3

ASSUMING #4 BARS EACH WAY

Mu	Mu-		Mu+		b = $\frac{16(12)}{2} = 96$
	CS	MS	CS	MS	
DEPTH	3.75"	3.75"	3.75"	3.75"	
Mn = Mu/φ	23.9 <sup>19</sup>	7.98 <sup>19</sup>	10.86 <sup>19</sup>	6.38 <sup>19</sup>	
FLEXURAL RESIST. FACTOR $R = \frac{Mn(12000)}{bd^2}$	212.5 PSI	20.93 PSI	96.53 PSI	56.71 PSI	
ROUNDRATIO TABLES	0.00375	0.00125	0.00175	0.0012	
As = ρbd	1.35	0.45	0.63	0.432	
Asmin = 0.0026T	0.96 in <sup>2</sup>	0.96 in <sup>2</sup>	0.96 in <sup>2</sup>	0.96 in <sup>2</sup>	
NUMBER OF BARS $N = \frac{As}{As(min)}$	6.75 → 7	2.25 → 3	3.15 → 4	2.16 → 3	
MIN BARS %	9.6 → 10	10	10	10	→ GOVERNS
SPACING S = ρd	9.5"	9.5"	9.5"	9.5"	
REINFORCEMENT	#4 @ 9.5" OC →				

DESIGN SHEAR REIN. FOR PUNCHING SHEAR

SHEAR PERIMETER:

$$\frac{d}{2} = 1.875 \quad b_o = 23.75 \times 4 = 95 \text{ in}$$

FACTORED LOAD INT. COL:  $1.2(92.5) + 1.6(100) = 271 \text{ PSF}$

$$V_u = 271(16^2 - 2^2) = 68,292 \text{ lbs}$$

NO SHEAR REIN.:

$$k = 0.75(4)\sqrt{3000} \times 95 = 3.75 = 58,537 < 68,292 - \text{NO GOOD}$$

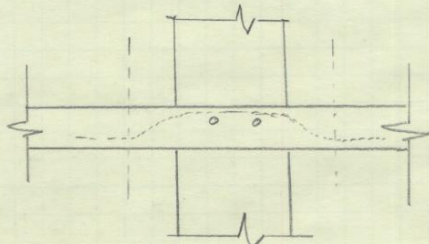
W/ 45° SHEAR BARS CONCL. CONTRIBUTION:

$$\phi V_c = 0.75(2)\sqrt{3000} \times 95 \times 3.75 = 29268.9$$

$$V_s = \frac{68292 - 29268.9}{.75} = 52030.8$$

$$A_v = \frac{52030.8}{60000 \sin 45} = 1.35 \text{ in}^2$$

2 BARS EACH DIRECTION #4 BARS  
AREA PER BAR =  $1.35/8 = 0.17$



NEW SHEAR PERIMETER

CRITICAL SEC:  $3.75 \text{ in}$   
 $27.5 \times 4 = 110$

$$V_u = 271(16^2 - 2.75^2) = 67,326.6$$

$$\phi V_c = 0.75(4)\sqrt{3000}(110) \times (3.75) = 67782 \checkmark$$



2 x 12" DECK  $F_y = 33\text{ksi}$   $f'_c = 3\text{ksi}$  115 pcf concrete



**L, Uniform Live Service Loads, psf \***

Slab Depth	$\phi_{Mn}$ in. k	6.00	6.50	7.00	7.50	8.00	8.50	9.00	9.50	10.00	10.50	11.00	11.50	12.00	
22 gage	4.50	40.27	400	370	315	270	235	205	180	160	140	125	110	100	90
	5.00	46.44	400	400	365	315	270	240	210	185	165	145	130	115	105
	5.25	49.53	400	400	390	335	290	255	225	195	175	155	140	125	110
	5.50	52.61	400	400	400	355	310	270	235	210	185	165	150	130	120
	6.00	58.78	400	400	400	400	345	300	265	235	210	185	165	150	135
	6.25	61.87	400	400	400	400	365	320	280	245	220	195	175	155	140
20 gage	4.50	64.95	400	400	400	400	380	335	295	260	230	205	185	165	145
	5.00	71.12	400	400	400	400	400	365	320	285	250	225	200	180	160
	5.25	74.20	400	400	400	400	385	335	295	260	230	205	185	165	145
	5.50	77.28	400	400	400	400	400	360	315	275	245	220	195	175	155
	6.00	83.45	400	400	400	400	400	380	335	295	260	230	205	185	165
	6.25	86.53	400	400	400	400	400	390	345	310	275	245	220	200	180
19 gage	4.50	89.61	400	400	400	400	400	400	365	325	290	255	230	210	185
	5.00	95.78	400	400	400	400	400	400	355	315	280	255	230	210	185
	5.25	98.86	400	400	400	400	385	335	295	260	230	205	185	165	150
	5.50	101.94	400	400	400	400	400	390	345	310	275	245	220	200	180
	6.00	108.11	400	400	400	400	400	400	390	345	310	275	245	220	200
	6.25	111.19	400	400	400	400	400	400	400	360	320	290	260	235	210
18 gage	4.50	114.27	400	400	400	400	400	400	380	340	305	275	245	225	205
	5.00	120.44	400	400	400	400	400	400	400	370	335	300	270	245	225
	5.25	123.52	400	400	400	400	400	375	330	290	260	230	210	185	170
	5.50	126.60	400	400	400	400	400	400	390	345	305	275	245	220	200
	6.00	132.77	400	400	400	400	400	400	400	360	320	290	260	235	210
	6.25	135.85	400	400	400	400	400	400	400	380	340	305	275	245	225
16 gage	4.50	138.93	400	400	400	400	400	400	400	400	370	335	300	270	245
	5.00	145.10	400	400	400	400	400	400	400	400	360	325	290	260	235
	5.25	148.18	400	400	400	400	400	400	390	345	305	275	245	220	200
	5.50	151.26	400	400	400	400	400	400	400	385	345	310	280	250	230
	6.00	157.43	400	400	400	400	400	400	400	400	365	325	295	265	240
	6.25	160.51	400	400	400	400	400	400	400	400	385	345	310	280	255

- 1 STUD/FT.
- NO STUDS

\* The Uniform Live Loads are based on the LRFD equation  $\phi M_n = (1.6L + 1.2D)/\phi$ . Although there are other load combinations that may require investigation, this will control most of the time. The equation assumes there is no negative bending reinforcement over the beams and therefore each composite slab is a single span. Two sets of values are shown;  $\phi M_n$  is used to calculate the uniform load when the full required number of studs is present;  $\phi M_{no}$  is used to calculate the load when no studs are present. A straight line interpolation can be done if the average number of studs is between zero and the required number needed to develop the "full" factored moment. The tabulated loads are checked for shear controlling (it seldom does), and also limited to a live load deflection of 1/360 of the span.

An upper limit of 400 psf has been applied to the tabulated loads. This has been done to guard against equating large concentrated to uniform loads. Concentrated loads may require special analysis and design to take care of serviceability requirements not covered by simply using a uniform load value. On the other hand, for any load combination the values provided by the composite properties can be used in the calculations.

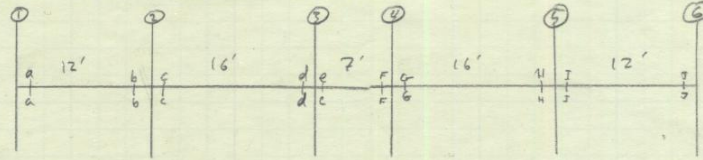
Welded wire fabric in the required amount is assumed for the table values. If welded wire fabric is not present, deduct 10% from the listed loads.

Refer to the example problems for the use of the tables.

**2" LOK-FLOOR**

①

2 WAY FLAT PLATE SLAB



SLAB THICKNESS

$$E_x = \frac{2l}{30} = \frac{16(12) - 2\%}{30} = 6.34 = 6.5''$$

$$INT = \frac{2l}{35} = 5.76 \Rightarrow \text{USE } 6.5'' \text{ TO KEEP UNIFORMITY}$$

$$DL: \quad 6.5 \left( \frac{150}{12} \right) = 81.25$$

$$1.2(111.25) + 1.6(100) = 293.5 \text{ PSF}$$

$$SI = 30.00$$

$$111.25$$

$$I_s = 16(12)(6.5^3)/12 = 4394 \text{ in}^4$$

$$K_{s(12)} = \frac{4E_c I_c}{2l - c\%} = \frac{4E_c(4394)}{12(12) - 2\%} = 131.2 E_c \text{ in}^3/\text{RAD}$$

$$K_{s(16)} = \frac{4E_c(4394)}{16(12) - 2\%} = 96.6 E_c$$

$$K_{s(7)} = \frac{4E_c(4394)}{7(12) - 2\%} = 237.5 E_c$$

$$20 \times 20 \text{ col } K_c = \frac{4E_c I_c}{L - 2c} = \frac{4E_c(20^4/12)}{(12)9.6 - 2(6.5)} = 521.9 E_c$$

$$\text{FLR Ht} = 9.66 \text{ FT}$$

$$C = \left( 1 + 1.63 \left( \frac{6.5}{20} \right) \right) \frac{6.5^3(20)}{3} = 2205.7$$

$$K_c = \frac{9E_c C}{L(1 - c\%)} = \frac{9E_c(2205.7)}{16(12)(1 - 2\%(12))} = 115.4 E_c$$

$$\frac{1}{K_{ec}} = \frac{1}{2 \cdot 521.9 E_c} + \frac{1}{2 \cdot 115.4 E_c} \Rightarrow K_{ec} = 189 E_c$$

DISTRIBUTION FACTORS

$$DF_{A-A, S-S} = \frac{131.2 E_c}{131.2 + 189} = 0.410$$

$$DF_{B-B, I-I} = \frac{131.2}{131.2 + 96.6 + 189} = 0.315$$

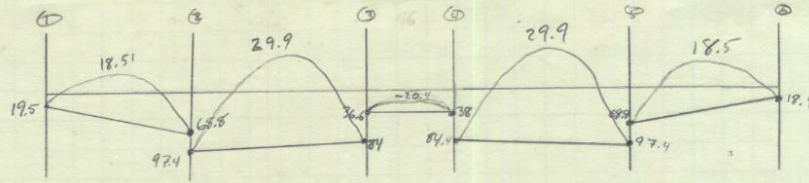
$$DF_{C-C, H-H} = \frac{96.6}{131.2 + 96.6 + 189} = 0.232$$

$$DF_{D-D, G-G} = \frac{96.6}{96.6 + 237.5 + 189} = 0.185$$

$$DF_{E-E, F-F} = \frac{237.5}{96.6 + 237.5 + 189} = 0.454$$



3



$$\frac{WR^2}{8} \Rightarrow \frac{293.4(16)(12 - \frac{16}{2})^2}{8} = 62.66 \text{ k}$$

$$\frac{293.4(16)(16 - \frac{16}{2})^2}{8} = 120.6 \text{ k}$$

$$\frac{293.4(16)(7 - \frac{16}{2})^2}{8} = 16.7 \text{ k}$$

Max  $M_u^- = 97.4$

Max  $M_u^+ = 29.9$

CS  $M_u^- = 0.75(97.4) = 73.1 \text{ k}$

MS  $M_u^- = 0.25(97.4) = 24.4 \text{ k}$

CS  $M_u^+ = 0.6(29.9) = 17.94 \text{ k}$

MS  $M_u^+ = 0.4(29.9) = 11.96 \text{ k}$

DESIGN REINFORCEMENT

	$M_u^-$		$M_u^+$	
	CS	MS	CS	MS
MOMENTS	73.1 k	24.4 k	17.94 k	11.96 k
EFF DEPTH (75% CLR) ASSUME				
#5 BARS BOTH DIRECTIONS	5.4375"	5.4375"	5.4375"	5.4375"
$M_n = M_u / \phi$	81.2 k	27.1 k	19.9 k	13.3 k
$R = M_n / b d^2$	309	103.2	75.89	50.6
REQ. RATIO $\rho$ (TABLES)	0.0055	0.0053	0.00125	0.0007
STEEL AREA $\phi b d$ (in <sup>2</sup> )	2.87	2.77	0.65	0.37
MIN STEEL AREA $A_{smin} = 0.0018 b t$ (in <sup>2</sup> )	1.13	1.13	1.13	1.13
# OF BARS $N = A_s / A_s \text{ BAR}$	(#5) 9.26 $\Rightarrow$ 10 BARS	(#5) 8.93 9 BARS	(#4 BAR) 3.25 4 BARS	(#4) 1.85 USE 4 BARS
MIN # OF BARS $N_{min} = b / 2s$	7.38 = 8 BARS			
SPACING OF BARS $S = b / N$	9.6" $\rightarrow$ FOR UNIFORMITY		24"	24"
FINAL REINFORCEMENT	#5 @ 9.5"	#5 @ 9.5"	#4 @ 24"	#4 @ 24"

$\frac{16(12)}{2} = 96$

SHEAR REINF. CHECK

$\frac{d}{2} = 2.72 \quad b_o = 25.44 \times 4 = 102$

$V_u = 293.5 \text{ PSF}(16^2 - 2^2) = 73,962 \text{ lbs}$

$V_c = 0.75(4) \sqrt{3000} (102)(5.4375) = 92181 > V_u \rightarrow$  No EXTRA SHEAR REIN. REQ'D

Span c-c. Columns $\ell_1 = \ell_2$ (ft)		Factored Super- imposed Load (psf)		(1) Steel (psf) $c_1 = c_2$ (in.)		Square Edge Column (2) Stirrups		Rib Depth = 8 in. Total Slab Depth = 3 in.		Reinforcing Bars—Each Direction		Middle Strip		Square Interior Panels		Reinforcing Bars—Each Direction		Total Slab Depth = 11 in.		Rib Depth = 8 in.		Total Slab Depth = 3 in.																									
																								Square Edge Column $c_1 = c_2$ (in.)		Square Interior Column (2) Stirrups		Moments +M Bot. (ft-k) -M Int. (ft-k)		Column Strip		Middle Strip		Square Interior Column $c_1 = c_2$ (in.)		Square Interior Column (2) Stirrups		Moment Strip		Square Interior Column $c_1 = c_2$ (in.)		Square Interior Column (2) Stirrups		Square Interior Column $c_1 = c_2$ (in.)		Square Interior Column (2) Stirrups	
14'-0" D= 6.417 RIB NOT ON COLUMN LINE 0.598 CF/SF	50 100 150 200 300 400	2.25 2.25 2.25 2.25 2.25	12 12 12 12 12	10-#5+0 10-#5+0 10-#5+0 10-#5+0 10-#5+0	4 4 4 4 4	2-#4 2-#4 2-#4 2-#4 2-#4	4 4 4 4 4	10-#5 10-#5 10-#5 10-#5 10-#5	3 3 3 3 3	#4 #4 #4 #4 #4	Bottom No. Long Bars	Top Interior No. Short Bars	Bottom No. Long Bars	Top Interior No. Short Bars	3 3 3 3 3	#4 #4 #4 #4 #4	4-#5 4-#5 4-#5 4-#5 4-#5	34 26 35 48 60 84 107	13 17 20 24 32 40	4-#5 4-#5 4-#5 4-#5 4-#5 4-#5	4 4 4 4 4	2-#4 2-#4 2-#4 2-#4 2-#4	4 4 4 4 4	10-#5 10-#5 10-#5 10-#5 10-#5	3 3 3 3 3	#4 #4 #4 #4 #4	4-#5 4-#5 4-#5 4-#5 4-#5																				
16'-0" D= 6.417 RIB NOT ON COLUMN LINE 0.562 CF/SF	50 100 150 200 300 400	2.30 2.30 2.30 2.30 2.30	12 12 12 12 12	12-#5+0 12-#5+0 12-#5+0 12-#5+0 12-#5+0	4 4 4 4 4	2-#4 2-#4 2-#4 2-#4 2-#4	4 4 4 4 4	12-#5 12-#5 12-#5 12-#5 12-#5	4 4 4 4 4	#4 #4 #4 #4 #4	Bottom No. Long Bars	Top Interior No. Short Bars	Bottom No. Long Bars	Top Interior No. Short Bars	4 4 4 4 4	#4 #4 #4 #4 #4	5-#5 5-#5 5-#5 5-#5 5-#5	52 31 99 126 162	19 25 37 48 60	5-#5 5-#5 5-#5 5-#5 5-#5	4 4 4 4 4	2-#4 2-#4 2-#4 2-#4 2-#4	4 4 4 4 4	12-#5 12-#5 12-#5 12-#5 12-#5	4 4 4 4 4	#4 #4 #4 #4 #4	5-#5 5-#5 5-#5 5-#5 5-#5																				
18'-0" D= 6.417 RIB NOT ON COLUMN LINE 0.571 CF/SF	50 100 150 200 300 400	2.25 2.25 2.33 2.58 2.84	12 12 12 12 12	13-#5+0 13-#5+0 13-#5+0 13-#5+0 13-#5+0	4 4 4 4 4	2-#4 2-#4 2-#4 1-#4 and 1-#5 2-#5	4 4 4 4 4	13-#5 13-#5 13-#5 13-#5 13-#5	5 5 5 5 5	#4 #4 #4 #4 #5	Bottom No. Long Bars	Top Interior No. Short Bars	Bottom No. Long Bars	Top Interior No. Short Bars	4 4 4 4 4	#4 #4 #4 #4 #4	5-#5 5-#5 5-#5 5-#5 5-#5	74 55 75 103 130 182 233	28 36 44 70 87	5-#5 5-#5 5-#5 5-#5 5-#5	4 4 4 4 4	2-#4 2-#4 2-#4 1-#4 and 1-#5 2-#5	4 4 4 4 4	13-#5 13-#5 13-#5 13-#5 13-#5	5 5 5 5 5	#4 #4 #4 #4 #4	5-#5 5-#5 5-#5 5-#5 5-#5																				
20'-0" D= 8.417 RIB ON COLUMN LINE 0.590 CF/SF	50 100 150 200 300 400	2.28 2.28 2.36 2.45 2.60 3.48	12 12 12 12 12 14	15-#5+0 15-#5+0 15-#5+0 15-#5+0 15-#5+0	5 5 5 5 5	2-#4 2-#4 1-#4 and 1-#5 2-#5 1-#6 and 1-#7	5 5 5 5 5	15-#5 15-#5 15-#5 15-#5 15-#5	5 5 5 5 5	#4 #4 #4 #4 #5	Bottom No. Long Bars	Top Interior No. Short Bars	Bottom No. Long Bars	Top Interior No. Short Bars	5 5 5 5 5	#4 #4 #4 #4 #4	6-#5 6-#5 6-#5 6-#5 6-#5	78 105 145 182 254 323	39 62 74 97 120	6-#5 6-#5 6-#5 6-#5 6-#5	5 5 5 5 5	2-#4 2-#4 2-#4 1-#4 and 1-#5 2-#5	5 5 5 5 5	15-#5 15-#5 15-#5 15-#5 15-#5	5 5 5 5 5	#4 #4 #4 #4 #4	6-#5 6-#5 6-#5 6-#5 6-#5																				
22'-0" D= 8.417 RIB ON COLUMN LINE 0.579 CF/SF	50 100 150 200 300 400	2.25 2.25 2.40 2.56 3.26 3.87	12 12 12 12 14 18	16-#5+0 16-#5+0 16-#5+0 16-#5+0 16-#5+0	5 5 5 5 5	2-#4 2-#4 2-#5 1-#5 and 1-#6 1-#6 and 1-#7	5 5 5 5 5	16-#5 16-#5 16-#5 16-#5 16-#5	6 6 6 6 6	#4 #4 #4 #4 #5	Bottom No. Long Bars	Top Interior No. Short Bars	Bottom No. Long Bars	Top Interior No. Short Bars	5 5 5 5 5	#4 #4 #4 #4 #4	7-#5 7-#5 7-#5 7-#5 7-#5	103 140 193 224 267 349	52 83 99 130 156	7-#5 7-#5 7-#5 7-#5 7-#5	5 5 5 5 5	2-#4 2-#4 2-#5 1-#5 and 1-#6 1-#6 and 1-#7	5 5 5 5 5	16-#5 16-#5 16-#5 16-#5 16-#5	6 6 6 6 6	#4 #4 #4 #4 #4	7-#5 7-#5 7-#5 7-#5 7-#5																				

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